

Integrability, Poisson-Lie Symmetry and Double Field Theory

Falk Hassler

University of North Carolina at Chapel Hill
University of Pennsylvania

based on

work in progress, 1707.08624, 1611.07978

and

1502.02428 with Pascal du Bosque, Dieter Lüst and Ralph Blumenhagen

May 1st, 2018

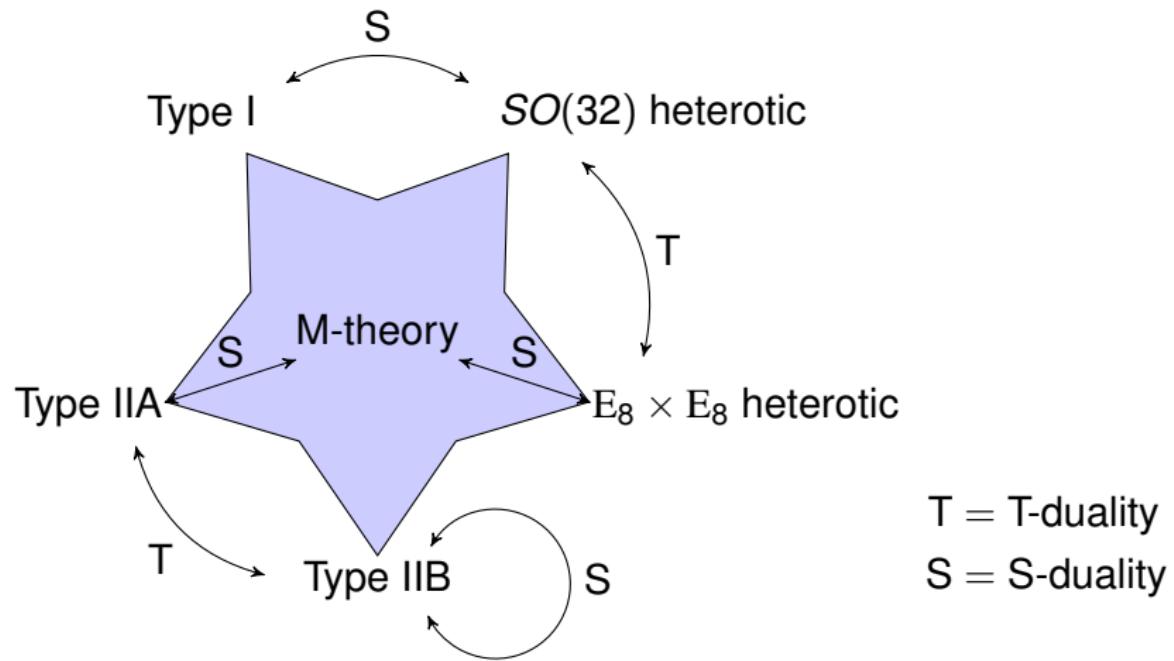
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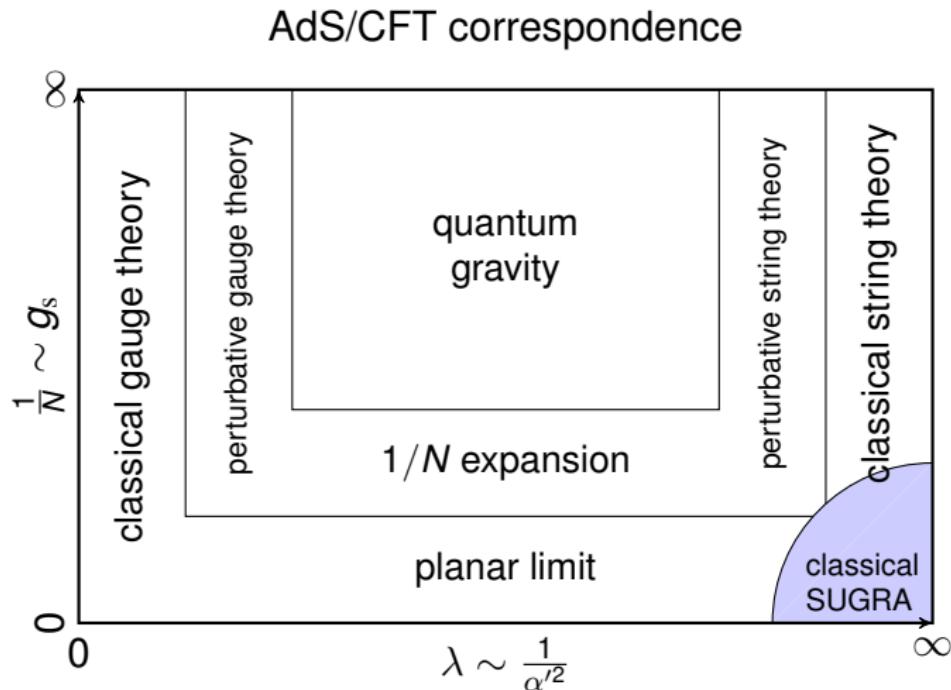
Holography, Strings and Exceptional/Double Field Theory

Canonical motivation for Exception/Double Field Theory



Holography, Strings and Exceptional/Double Field Theory

But there is also another interesting story...



Outline

1. Motivation

2. Integrability and AdS/CFT

3. Poisson-Lie Symmetry

4. Double Field Theory on Drinfeld doubles

5. Summary

Integrability

or how to “solve” 4D maximal SYM
completely

Anomalous dimension in 4D $\mathcal{N} = 4$ SYM

- ▶ CFT two point function of primaries

$$\langle \mathcal{O}_i(x) \mathcal{O}_j(y) \rangle = \frac{\delta_{ij}}{|x - y|^{2\Delta}}$$

- ▶ scaling dimension gets renormalized

$$\Delta = \Delta_0 + \lambda \Delta_1 + \dots$$

- ▶ example single trace operator $\text{Tr } Z^L \quad Z = \frac{1}{\sqrt{2}}(\phi_1 + i\phi_2)$

$$S = \int d^4x \text{Tr} \left(-\frac{1}{4}F_{\mu\nu}F^{\mu\nu} - \frac{1}{2}D_\mu\phi_i D^\mu\phi^i - \frac{g^2}{4}[\phi_i, \phi_j][\phi^i, \phi^j] + \text{fermions} \right)$$

- ▶ $\Delta_0 = L$ what about Δ_1, \dots

- ▶ more general single trace operators with $(L - M) \times Z$ and $M \times W = \frac{1}{\sqrt{2}}(\phi_3 + i\phi_4)$

SU(2) spin chain and the Bethe ansatz

- $\Delta_1 \leftrightarrow$ eigenvalues of the Heisenberg spin chain

$$H = 2 \sum_{I=1}^L \left(\frac{1}{4} - \vec{S}_I \cdot \vec{S}_{I+1} \right) \quad S_I = \frac{1}{2} \vec{\sigma}_I$$

$Z = \uparrow$, $W = \downarrow$, and for $L = 3$ $\text{Tr } ZZW = |\uparrow\uparrow\downarrow\rangle$

- Bethe ansatz gives rise to eigenvalues and vectors
- just possible because spin chain is **integrable**
- integrability is so powerful that it also finds all corrections

$\Delta_1, \Delta_2, \Delta_3 \dots$

Where is the integrability in string theory?

Ingredients for classical/quantum integrability:

1. Hamiltonian/Hamilton operator
2. Poisson-bracket/commutator
3. Lax pair

► example Principal Chiral Model (PCM)

$$S = \frac{1}{2} \int d^2\sigma \text{Tr}(g^{-1} \partial_+ g g^{-1} \partial_- g)$$

$$H = \frac{1}{2} \int d\sigma \text{Tr}(j_0^2 + j_1^2) \quad j_0 = g^{-1} \partial_\tau g \quad j_1 = g^{-1} \partial_\sigma g$$

$$\{j_{0\,a}(\sigma), j_{0\,b}(\sigma')\} = f_{ab}{}^c j_{0\,c} \qquad A_\pm(\lambda) = \frac{j_0 \pm j_1}{1 \pm \lambda}$$

$$\{j_{0\,a}(\sigma), j_{1\,b}(\sigma')\} = f_{ab}{}^c j_{1\,c} + \delta_{ab}$$

$$\{j_{1\,a}(\sigma), j_{1\,b}(\sigma')\} = 0$$

Let's generalize this construction!

- ▶ Hamiltonian (Poisson-Lie σ -model) :

$$H = \frac{1}{2} \int d\sigma j_A(\sigma) \mathcal{H}^{AB} j_B(\sigma)$$

- ▶ Poisson-bracket:

$$\{j_A(\sigma), j_B(\sigma')\} = F_{AB}{}^C j_C(\sigma) \delta(\sigma - \sigma') + \eta_{AB} \delta'(\sigma - \sigma')$$

- ▶ Lax pair:

$$A_{\pm}(\lambda) = \frac{\mathcal{J} \pm \mathcal{R}}{1 \pm \lambda}$$

Many known integrable 2D non-linear σ -models can be brought in this form. They are fixed completely by specifying the **constants** \mathcal{H}^{AB} and $F_{AB}{}^C$.

Examples:

- ▶ η -deformation
 - ▶ with/without WZW term
 - ▶ on group manifolds
 - ▶ and coset spaces
- ▶ λ -deformation

Poisson-Lie symmetry

Poisson as in Poisson-bracket:
required for the Hamilton formalism

Lie as in Lie-algebra:
e.g. required for Lax's equation
 $\partial_+ A_-(\lambda) - \partial_- A_+(\lambda) + [A_-(\lambda), A_+(\lambda)] = 0$

Drinfeld double [Drinfeld, 1988]

Definition: A **Drinfeld double** is a $2D$ -dimensional Lie group \mathcal{D} , whose Lie-algebra \mathfrak{d}

1. has an ad-invariant bilinear for $\langle \cdot, \cdot \rangle$ with signature (D, D)
2. admits the decomposition into two maximal isotropic subalgebras \mathfrak{g} and $\tilde{\mathfrak{g}}$

- ▶ $(t^a \quad t_a) = t_A \in \mathfrak{d}, \quad t_a \in \mathfrak{g} \quad \text{and} \quad t^a \in \tilde{\mathfrak{g}}$
- ▶ $\langle t_A, t_B \rangle = \eta_{AB} = \begin{pmatrix} 0 & \delta_b^a \\ \delta_a^b & 0 \end{pmatrix}$
- ▶ $[t_A, t_B] = F_{AB}{}^C t_C$ with non-vanishing commutators

$$[t_a, t_b] = f_{ab}{}^c t_c \qquad [t_a, t^b] = \tilde{f}^{bc}{}_a t_c - f_{ac}{}^b t^c$$

$$[t^a, t^b] = \tilde{f}^{ab}{}_c t^c$$

- ▶ ad-invariance of $\langle \cdot, \cdot \rangle$ implies $F_{ABC} = F_{[ABC]}$

Poisson-Lie Symmetry [Klimcik and Severa, 1995]

- ▶ 2D σ -model on target space M with action

$$S(E, M) = \int dz d\bar{z} E_{ij} \partial x^i \bar{\partial} x^j$$

- ▶ $E_{ij} = g_{ij} + B_{ij}$ captures metric and two-form field on M
- ▶ inverse of E_{ij} is denoted as E^{ij}
- ▶ left invariant vector field $v_a{}^i$ on G is the inverse transposed of right invariant Maurer-Cartan form $t_a v^a{}_i dx^i = dg g^{-1}$
- ▶ adjoint action of $g \in G$ on $t_A \in \mathfrak{o}$: $\text{Ad}_g t_A = g t_A g^{-1} = M_A{}^B t_B$
- ▶ analog for \tilde{G}

Definition: $S(E, \mathcal{D}/\tilde{G})$ has **Poisson-Lie Symmetry** if

$$J_a = -v_a{}^i E_{ji} \partial x^j dz + v_a{}^i E_{ij} \bar{\partial} x^j d\bar{z}$$

is a conserved non-commutative Noether current

$$(dJ_a - \frac{1}{2} F^{bc} {}_a J_b \wedge J_c = 0).$$

Poisson-Lie Symmetry [Klimcik and Severa, 1995]

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Definition: $S(E, \mathcal{D}/\tilde{G})$ has **Poisson-Lie Symmetry** if

$$L_{v_a} E_{ij} = -F^{bc}{}_a v_b{}^k v_c{}^l E_{ik} E_{lj}$$

holds.

Poisson-Lie Symmetry [Klimcik and Severa, 1995]

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Definition: $S(E, \mathcal{D}/\tilde{G})$ has **Poisson-Lie Symmetry** if

$$E^{ij} = v_c{}^i M_a{}^c (M^{ae} M^b{}_e + E_0^{ab}) M_b{}^d v_d{}^j$$

holds, where E_0^{ab} is constant and invertible with the inverse $E_0{}_{ab}$.

Immediate consequence: Poisson-Lie T-duality

- exchanging G and \tilde{G} results in dual σ -model with

$$\tilde{E}^{ij} = \tilde{\nu}^{ci} \tilde{M}^a{}_c (\tilde{M}_{ae} \tilde{M}_b{}^e + E_{0\,ab}) \tilde{M}^b{}_d \tilde{\nu}^{dj}$$

- captures $\begin{cases} \text{abelian T-d.} & G \text{ abelian and } \tilde{G} \text{ abelian} \\ \text{non-abelian T-d.} & G \text{ non-abelian and } \tilde{G} \text{ abelian} \end{cases}$
[Ossa and Quevedo, 1993; Giveon and Rocek, 1994; Alvarez, Alvarez-Gaume, and Lozano, 1994; ...]

- dual σ -models related by canonical transformation

[Klimcik and Severa, 1995; Klimcik and Severa, 1996; Sfetsos, 1998]

- equivalent at the classical level

- preserves conformal invariance at one-loop

[Alekseev, Klimcik, and Tseytlin, 1996; Sfetsos, 1998; ...; Jurco and Vysoky, 2017]

- dilaton transformation [Jurco and Vysoky, 2017]

$$\phi = -\frac{1}{2} \log \left| \det \left(1 + \tilde{g}_0^{-1} (\tilde{B}_0 + \Pi) \right) \right|$$
$$\tilde{\phi} = -\frac{1}{2} \log \left| \det \left(1 + g_0^{-1} (B_0 + \tilde{\Pi}) \right) \right|$$

SUGRA

- ▶ DFT makes PL-Symmetry manifest
- ▶ consistent tractions are central
- ▶ get the dialton, R/R sector nearly for free

Additional structure on the Drinfeld double

[Blumenhagen, Hassler, and Lüst, 2015, Blumenhagen, Bosque, Hassler, and Lüst, 2015]

- ▶ right invariant vector $E_A{}^I$ field on \mathcal{D} is the inverse transposed of left invariant Maurer-Cartan form $t_A E^A{}_I dX^I = g^{-1} dg$
- ▶ two η -compatible, covariant derivatives¹
 1. flat derivative

$$D_A V^B = E_A{}^I \partial_I V^B - w F_A V^B, \quad F_A = D_A \log |\det(E^B{}_I)|$$

2. convenient derivative

$$\nabla_A V^B = D_A V^B + \frac{1}{3} F_{AC}{}^B V^C$$

- ▶ generalized metric \mathcal{H}_{AB} ($w = 0$)

$$\mathcal{H}_{AB} = \mathcal{H}_{(AB)}, \quad \mathcal{H}_{AC} \eta^{CD} \mathcal{H}_{DB} = \eta_{AB}$$

- ▶ generalized dilaton d with e^{-2d} scalar density of weight $w = 1$
- ▶ triple $(\mathcal{D}, \mathcal{H}_{AB}, d)$ captures the doubled space of DFT

¹definitions here just for quantities with flat indices

Double Field Theory for $(\mathcal{D}, \mathcal{H}_{AB}, d)$ [Blumenhagen, Bosque, Hassler, and Lüst, 2015]

see also [Vaisman, 2012; Hull and Reid-Edwards, 2009; Geissbuhler, Marques, Nunez, and Penas, 2013; Cederwall, 2014; ...]

- ▶ action ($\nabla_A d = -\frac{1}{2} e^{2d} \nabla_A e^{-2d}$)

$$S_{\text{NS}} = \int_{\mathcal{D}} d^{2D} X e^{-2d} \left(\frac{1}{8} \mathcal{H}^{CD} \nabla_C \mathcal{H}_{AB} \nabla_D \mathcal{H}^{AB} - \frac{1}{2} \mathcal{H}^{AB} \nabla_B \mathcal{H}^{CD} \nabla_D \mathcal{H}_{AC} \right. \\ \left. - 2 \nabla_A d \nabla_B \mathcal{H}^{AB} + 4 \mathcal{H}^{AB} \nabla_A d \nabla_B d + \frac{1}{6} F_{ACD} F_B{}^{CD} \mathcal{H}^{AB} \right)$$

- ▶ generalized diffeomorphisms

$$\mathcal{L}_\xi V^A = \xi^B \nabla_B V^A + (\nabla^A \xi_B - \nabla_B \xi^A) V^B + w \nabla_B \xi^B V^A$$

- ▶ 2D-diffeomorphisms

$$L_\xi V^A = \xi^B D_B V^A + w D_B \xi^B V^A$$

- ▶ global O(D,D) transformations

$$V^A \rightarrow T^A{}_B V^B \quad \text{with} \quad T^A{}_C T^B{}_D \eta^{CD} = \eta^{AB}$$

- ▶ section condition (SC)

$$\eta^{AB} D_A \cdot D_B \cdot = 0$$

Symmetries of the action

► S_{NS} invariant for $X^I \rightarrow X^I + \xi^A E_A{}^I$ and

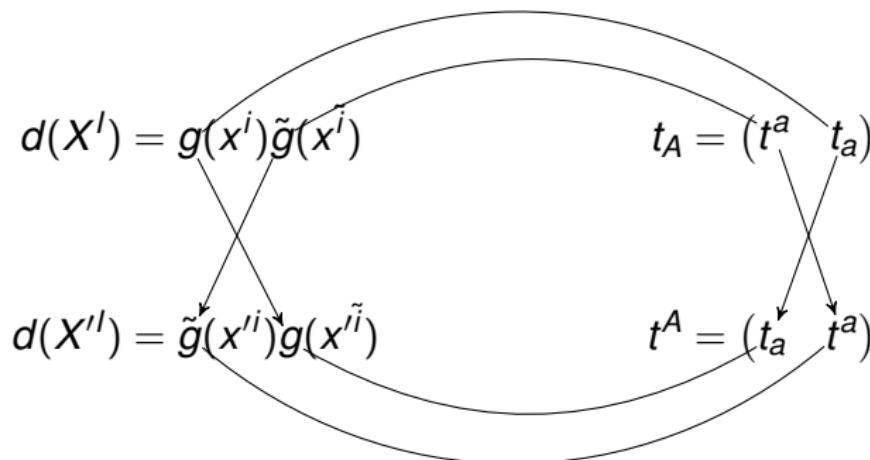
1. $\mathcal{H}^{AB} \rightarrow \mathcal{H}^{AB} + \mathcal{L}_\xi \mathcal{H}^{AB}$ and $e^{-2d} \rightarrow e^{-2d} + \mathcal{L}_\xi e^{-2d}$
2. $\mathcal{H}^{AB} \rightarrow \mathcal{H}^{AB} + L_\xi \mathcal{H}^{AB}$ and $e^{-2d} \rightarrow e^{-2d} + L_\xi e^{-2d}$

object	gen.-diffeomorphisms	2D-diffeomorphisms	global $O(D,D)$
\mathcal{H}_{AB}	tensor	scalar	tensor
$\nabla_A d$	not covariant	scalar	1-form
e^{-2d}	scalar density ($w=1$)	scalar density ($w=1$)	invariant
η_{AB}	invariant	invariant	invariant
$F_{AB}{}^C$	invariant	invariant	tensor
$E_A{}^I$	invariant	vector	1-form
S_{NS}	invariant	invariant	invariant
SC	invariant	invariant	invariant
D_A	not covariant	covariant	covariant
∇_A	not covariant	covariant	covariant

manifest

Poisson-Lie T-duality: 1. Solve SC [Hassler, 2016]

- ▶ fix D physical coordinates x^i from $X^I = \begin{pmatrix} x^i & x^{\tilde{i}} \end{pmatrix}$ on \mathcal{D}
such that $\eta^{IJ} = E_A{}^I \eta^{AB} E_B{}^J = \begin{pmatrix} 0 & \cdots \\ \cdots & \cdots \end{pmatrix} \rightarrow$ SC is solved
- ▶ fields and gauge parameter depend just on x^i
- ▶ only *two* SC solutions, relate them by symmetries of DFT



Poisson-Lie T-duality: 2. As manifest symmetry of DFT

- ▶ same structure as in the original paper [Klimcik and Severa, 1995]
- ▶ duality target spaces arise as different solutions of the SC

Poisson-Lie T-duality:

- ▶ 2D-diffeomorphisms $X^I \rightarrow X'^I (X^1, \dots X^{2D})$ with $d(X^I) = d(X'^I)$
- ▶ global $O(D,D)$ transformation $t_A \rightarrow \eta^{AB} t_B$

manifest symmetries of DFT

- ▶ for abelian T-duality $X^I \rightarrow X'^I = X^I$
- no 2D-diffeomorphisms needed, only global $O(D,D)$ transformation

Poisson-Lie Symmetry is a manifest symmetry of DFT

Equivalence to supergravity: 1. Generalized parallelizable spaces

[Lee, Strickland-Constable, and Waldram, 2014]

- ▶ generalized tangent space element $V^{\hat{I}} = (V^i \quad V_i)$
- ▶ generalized Lie derivative

$$\widehat{\mathcal{L}}_{\xi} V^{\hat{I}} = \xi^{\hat{J}} \partial_{\hat{J}} V^{\hat{I}} + (\partial^{\hat{I}} \xi_{\hat{J}} - \partial_{\hat{J}} \xi^{\hat{I}}) V^{\hat{J}} \quad \text{with} \quad \partial_{\hat{I}} = (0 \quad \partial_i)$$

Definition: A manifold M which admits a globally defined generalized frame field $\widehat{E}_A{}^{\hat{I}}(x^i)$ satisfying

1. $\widehat{\mathcal{L}}_{\widehat{E}_A} \widehat{E}_B{}^{\hat{I}} = F_{AB}{}^C \widehat{E}_C{}^{\hat{I}}$

where $F_{AB}{}^C$ are the structure constants of a Lie algebra \mathfrak{h}

2. $\widehat{E}_A{}^{\hat{I}} \eta^{AB} \widehat{E}_B{}^{\hat{J}} = \eta^{\hat{I}\hat{J}} = \begin{pmatrix} 0 & \delta_i^j \\ \delta_j^i & 0 \end{pmatrix}$

is a **generalized parallelizable space** $(M, \mathfrak{h}, \widehat{E}_A{}^{\hat{I}})$.

Equivalence to supergravity: 2. Generalized metric and dilaton

[Klimcik and Severa, 1995; Hull and Reid-Edwards, 2009; du Bosque, Hassler, Lüst, 2017]

- ▶ Drinfeld double $\mathcal{D} \rightarrow$ two generalized parallelizable spaces:

$$(\mathcal{D}/\tilde{G}, \mathfrak{o}, \hat{E}_A{}^{\hat{I}})$$

and

$$(\mathcal{D}/G, \mathfrak{o}, \tilde{\hat{E}}_A{}^{\hat{I}})$$

$$\hat{E}_A{}^{\hat{I}} = M_A{}^B \begin{pmatrix} v^b{}_i & 0 \\ 0 & v_b{}^i \end{pmatrix} {}_B{}^{\hat{I}}$$

$$\tilde{\hat{E}}_A{}^{\hat{I}} = \tilde{M}_{AB} \begin{pmatrix} \tilde{v}_{bi} & 0 \\ 0 & \tilde{v}^{bi} \end{pmatrix} {}^B{}^{\hat{I}}$$

- ▶ express \mathcal{H}^{AB} in terms of the generalized $\hat{\mathcal{H}}^{\hat{I}\hat{J}}$ on $TD/\tilde{G} \oplus T^*D/\tilde{G}$

$$\mathcal{H}^{AB} = \hat{E}_A{}_{\hat{I}} \hat{\mathcal{H}}^{\hat{I}\hat{J}} \hat{E}^B{}_{\hat{J}} \quad \text{with} \quad \hat{\mathcal{H}}^{\hat{I}\hat{J}} = \begin{pmatrix} g_{ij} - B_{ik}g^{kl}B_{lk} & -B_{ik}g^{kl} \\ g^{ik}B_{kj} & g^{ij} \end{pmatrix}$$

- ▶ express d in terms of the standard generalized dilaton \hat{d}

$$d = \hat{d} - \frac{1}{2} \log |\det \tilde{v}_{ai}|$$

$$\hat{d} = \phi - 1/4 \log |\det g_{ij}|$$

- ▶ plug into the DFT action S_{NS}

Equivalence to supergravity: 3. IIA/B bosonic sector action

- if G and \tilde{G} are unimodular

$$S_{\text{NS}} = V_{\tilde{G}} \int d^D x e^{-2\hat{d}} \left(\frac{1}{8} \hat{\mathcal{H}}^{\hat{K}\hat{L}} \partial_{\hat{K}} \hat{\mathcal{H}}_{\hat{I}\hat{J}} \partial_{\hat{L}} \hat{\mathcal{H}}^{\hat{I}\hat{J}} - 2 \partial_{\hat{I}} \hat{d} \partial_{\hat{J}} \hat{\mathcal{H}}^{\hat{I}\hat{J}} \right. \\ \left. - \frac{1}{2} \hat{\mathcal{H}}^{\hat{I}\hat{J}} \partial_{\hat{J}} \hat{\mathcal{H}}^{\hat{K}\hat{L}} \partial_{\hat{L}} \hat{\mathcal{H}}_{\hat{I}\hat{K}} + 4 \hat{\mathcal{H}}^{\hat{I}\hat{J}} \partial_{\hat{I}} \hat{d} \partial_{\hat{J}} \hat{d} \right)$$

- $V_{\tilde{G}} = \int_{\tilde{G}} d\tilde{x}^D \det \tilde{v}_{ai}$ volume of group \tilde{G} .

- equivalent to IIA/B NS/NS sector action

[Hohm, Hull, and Zwiebach, 2010; Hohm, Hull, and Zwiebach, 2010]

$$S_{\text{NS}} = V_{\tilde{G}} \int d^D x \sqrt{\det(g_{ij})} e^{-2\phi} (\mathcal{R} + 4\partial_i \phi \partial^i \phi - \frac{1}{12} H_{ijk} H^{ijk})$$

- holds for all $\mathcal{H}_{AB}(x^i) / \hat{\mathcal{H}}^{\hat{I}\hat{J}}$
- only D -diffeomorphisms and B -field gauge trans. as symmetries
- similar story for R/R sector

Restrictions on \mathcal{H}_{AB} and d to admit Poisson-Lie Symmetry

- ▶ in general $\mathcal{H}_{AB}(x^i) \xrightarrow{\text{Poisson-Lie T-duality (2D-diff.)}} \mathcal{H}_{AB}(x'^i, x^{\tilde{i}})$
- ▶ $x^{\tilde{i}}$ part not compatible with ansatz for SC solutions \rightarrow avoid it

A doubled space $(\mathcal{D}, \mathcal{H}_{AB}, d)$ admits Poisson-Lie T-dual supergravity descriptions iff

1. $L_\xi \mathcal{H}_{AB} = 0 \quad \forall \xi \quad \rightarrow \quad D_A \mathcal{H}_{AB} = 0$
2. $L_\xi d = 0 \quad \forall \xi \quad \rightarrow \quad D_A e^{-2d} = 0$

Application: Dilaton profile

► $D_A e^{-2d} = 0 \rightarrow \partial_I (\underbrace{2d + \log |\det v| + \log |\det \tilde{v}|}_{= 2\phi_0 = \text{const.}}) = 0$

► $d = \phi - \frac{1}{4} \log |\det g| - \frac{1}{2} \log |\det \tilde{v}| \rightarrow \phi = \phi_0 + \frac{1}{4} \log |\det g| - \frac{1}{2} \log |\det v|$

► $g = v^T e^T ev \quad \text{with} \quad \left\{ \begin{array}{l} (\tilde{B}_0 + \tilde{g}_0)^{ab} = E^{0\ ab} \\ \Pi^{ab} = M^{ac} M^b{}_c \\ e^{-1} e^{-T} = \tilde{g}_0 - (\tilde{B}_0 + \Pi) \tilde{g}_0^{-1} (\tilde{B}_0 + \Pi) \\ \tilde{e}_0^T \tilde{e}_0 = \tilde{g}_0 \\ e^{-T} = \tilde{e}_0 + \tilde{e}_0^{-T} (\tilde{B}_0 + \Pi) \end{array} \right.$

► $\phi = \phi_0 + \frac{1}{2} \log |\det e| = \phi_0 - \frac{1}{2} \log |\det \tilde{e}_0| - \frac{1}{2} \log |\det (1 + \tilde{g}_0^{-1} (\tilde{B}_0 + \Pi))|$

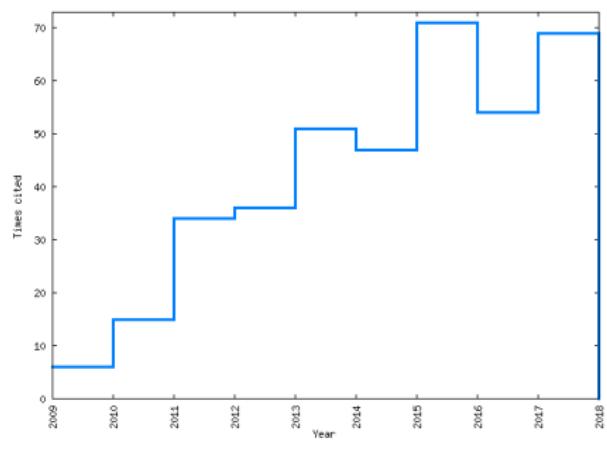
► reproduces [Jurco and Vysoky, 2017]

Summary

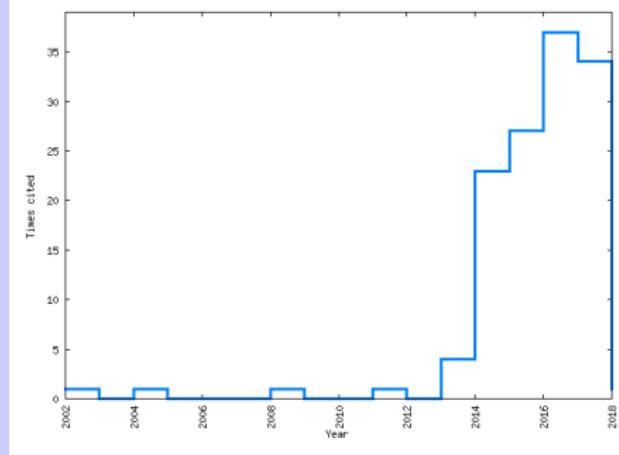
- ▶ DFT, Poisson-Lie T-duality and Drinfeld doubles fit together naturally
- ▶ interpretation of doubled space does not require winding modes anymore (phase space perspective instead)
- ▶ various new directions for research in DFT
 - ▶ connection to integrability in SUGRA
 - ▶ Drinfeld doubles → quantum groups → rich mathematical structure
 - ▶ new way to organized α' corrections?
 - ▶ implication for consistent truncation
 - ▶ branes in curved space [Klimcik, and Severa, 1996 (D-branes)]?
- ▶ facilitates new applications
 - ▶ integrable deformations of 2D σ -models
 - ▶ solution generating technique
 - ▶ explore underlying structure of AdS/CFT

Summary

- ▶ DFT, Poisson-Lie T-duality and Drinfeld doubles fit together naturally
- ▶ interpretation of doubled space does not require winding modes



Hull and Zwiebach, 2009



Klimcik, 2002

- ▶ solution generating technique
- ▶ explore underlying structure of AdS/CFT