

# Stringy Geometries in the Context of Double Field Theory

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based on a project with  
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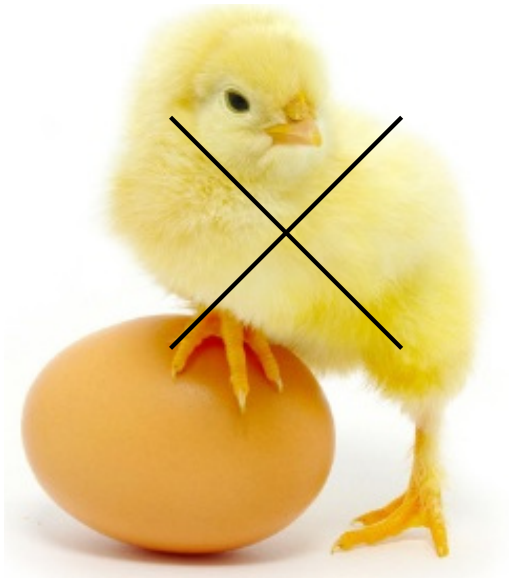
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3. describe strings moving in the **background**



String theory...



## ...and the string theory landscape [1].

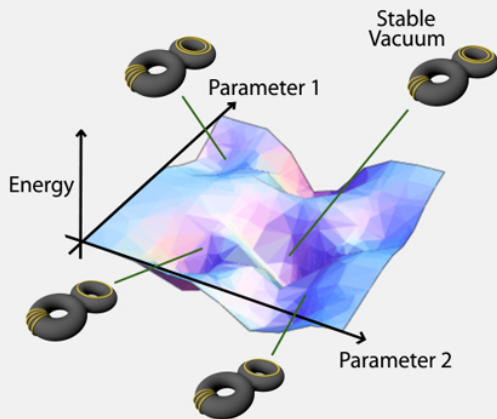
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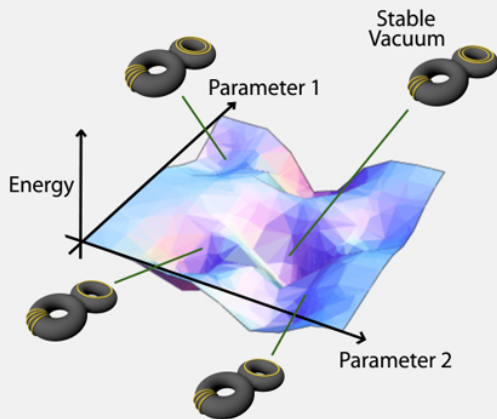
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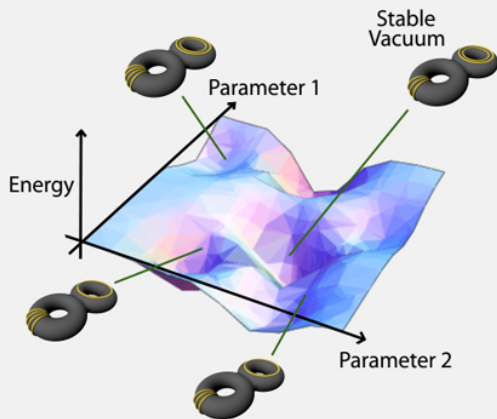
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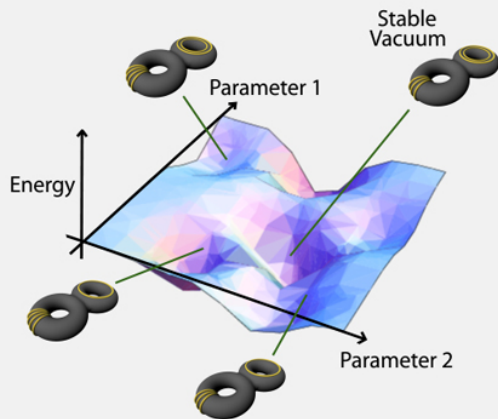
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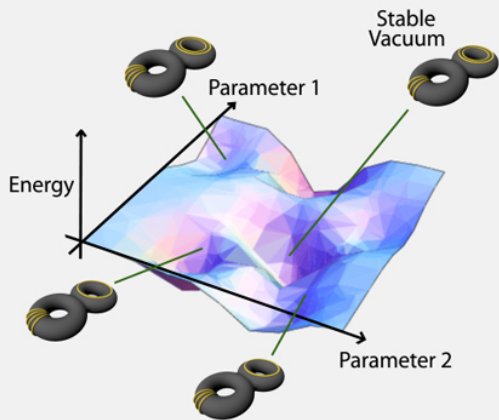
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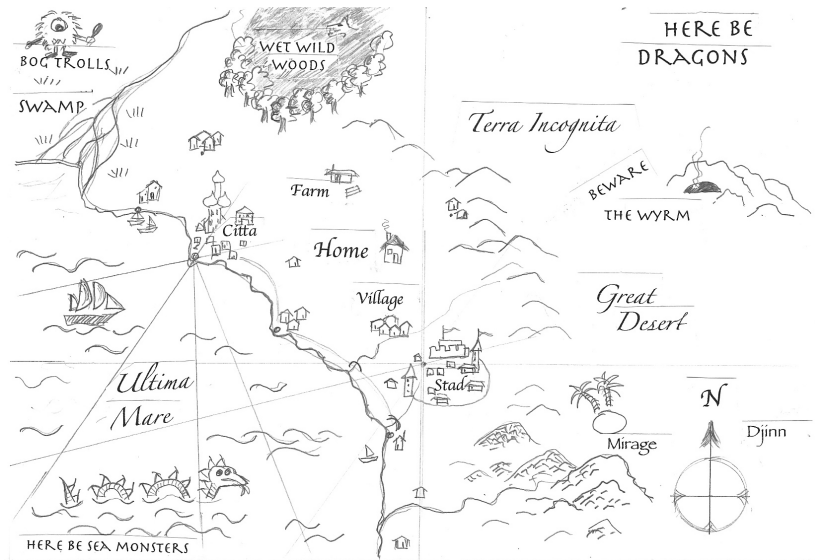
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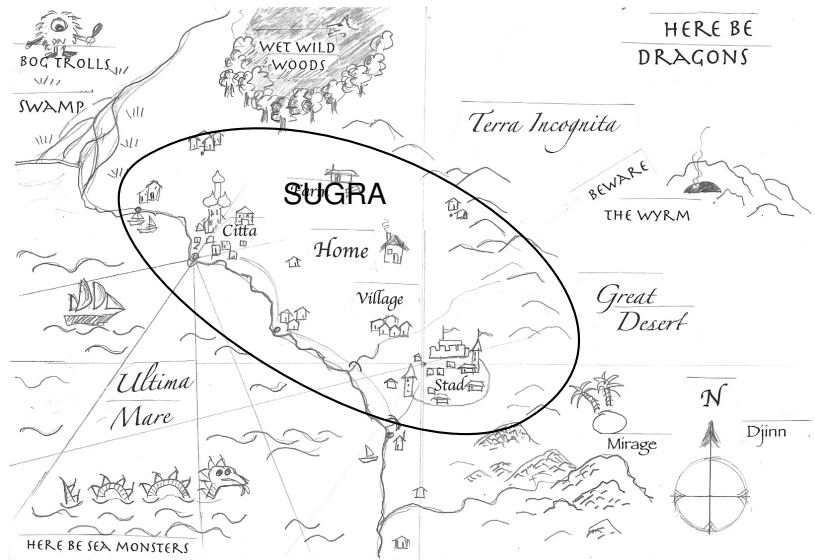
$10^{500}$  backgrounds  
[2, 3]



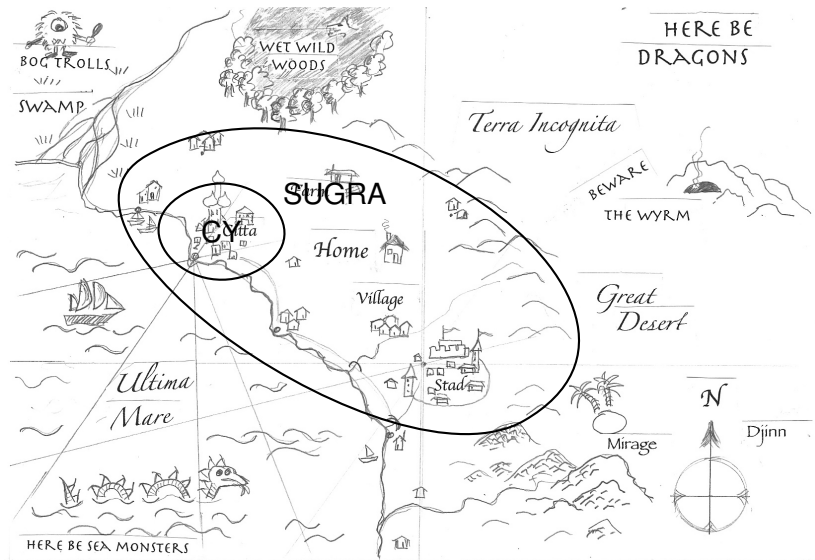
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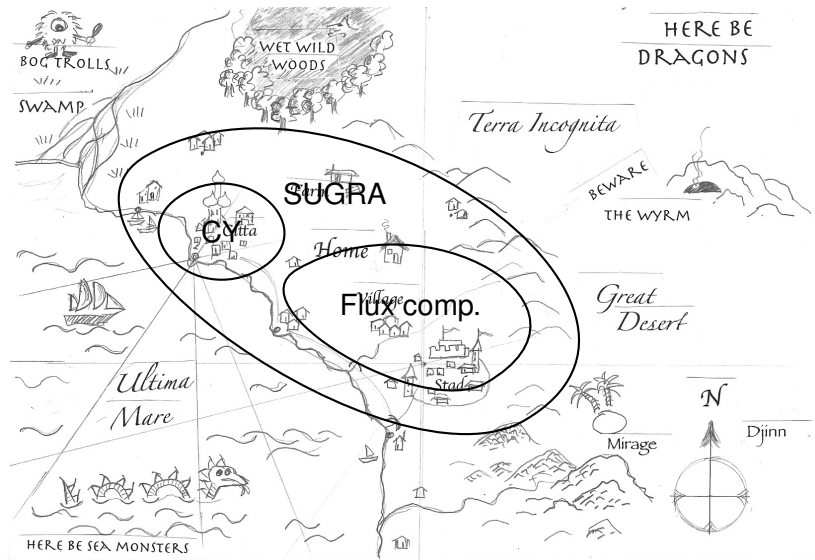
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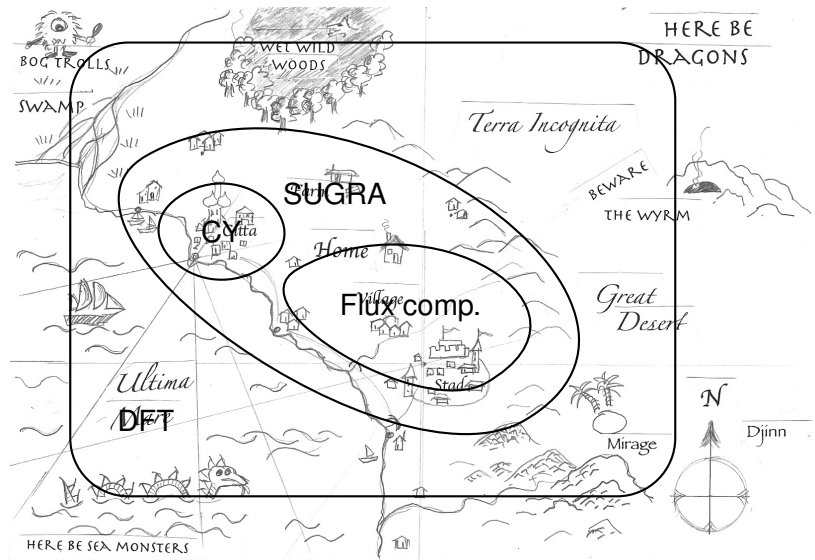
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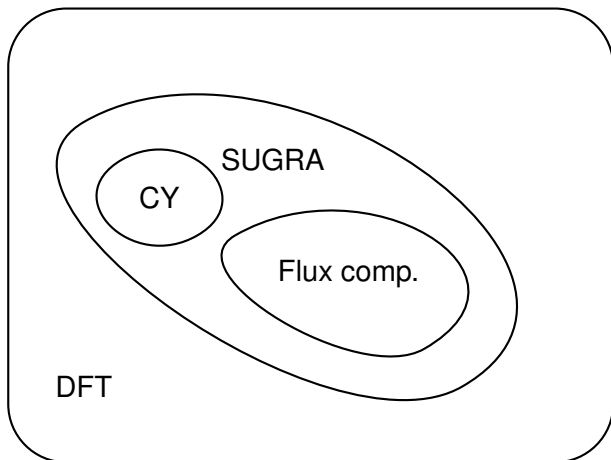
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$$S_{\text{NS}} = \int d^D x \sqrt{g} e^{-2\phi} \left( \mathcal{R} + 4\partial_\mu \phi \partial^\mu \phi - \frac{1}{12} H_{\mu\nu\rho} H^{\mu\nu\rho} \right)$$



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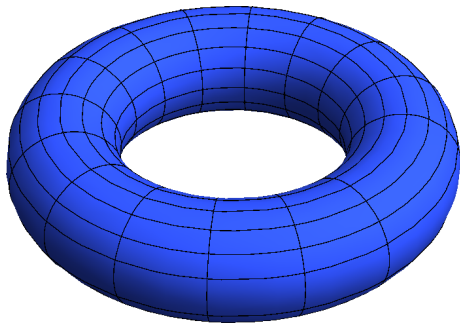
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- ▶ backgrounds solve  $S_{\text{NS}}$ 's field equations

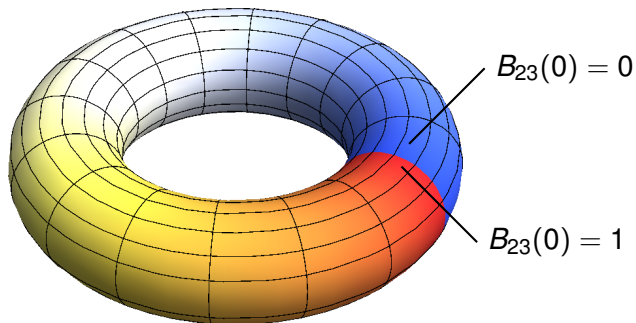
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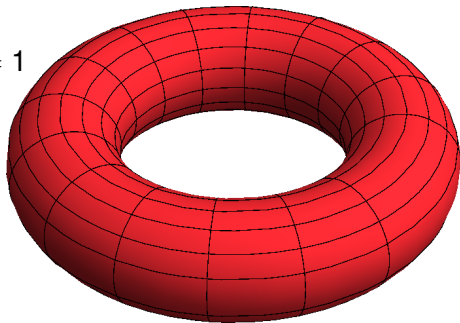


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$$H_{123} = \partial_{[1} B_{23]} = 1$$

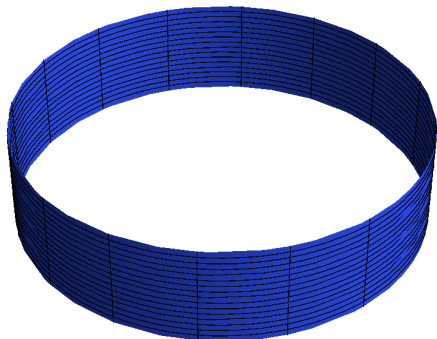


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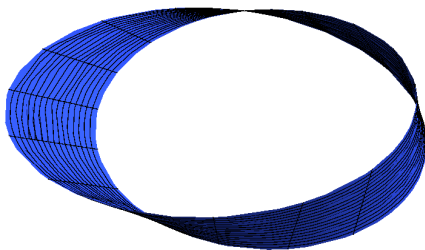
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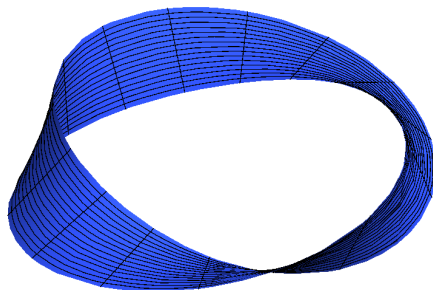
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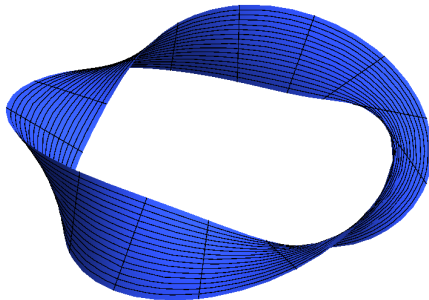
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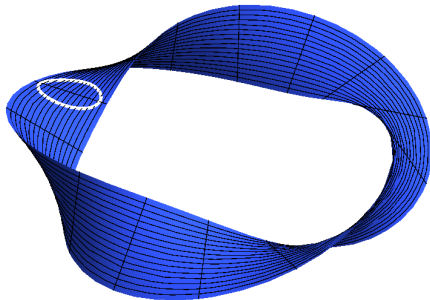
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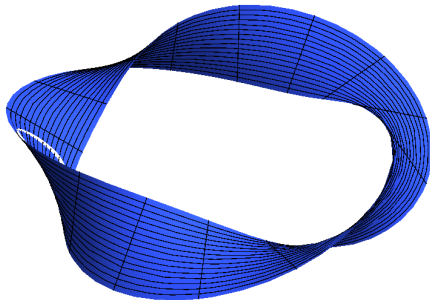
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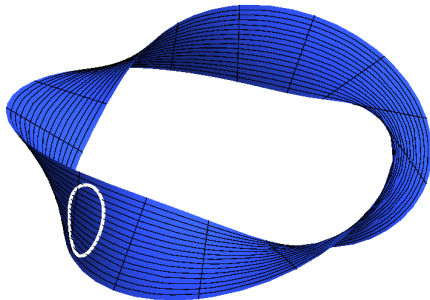
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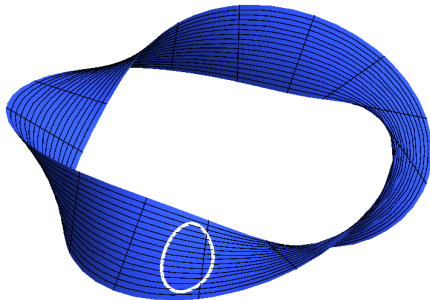
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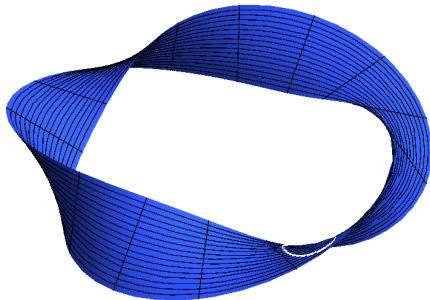


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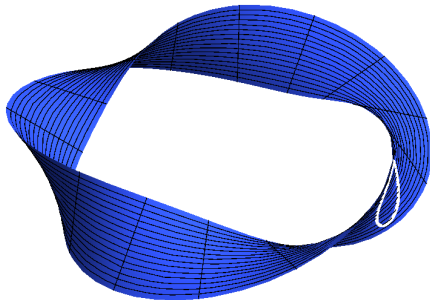
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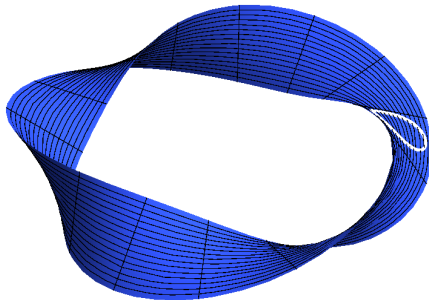
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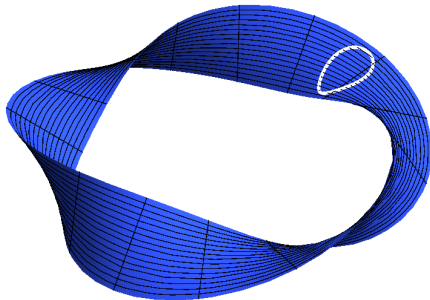
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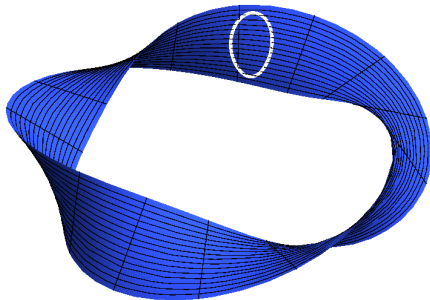
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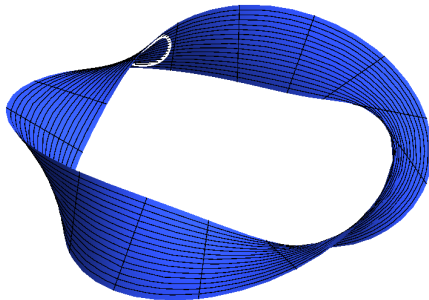
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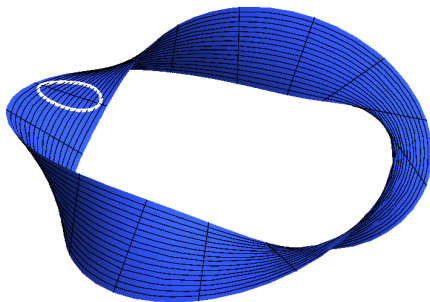
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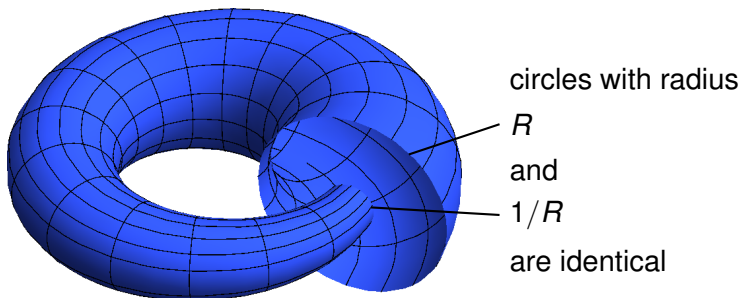
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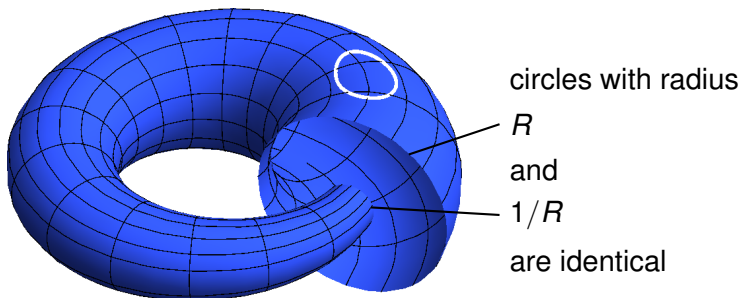
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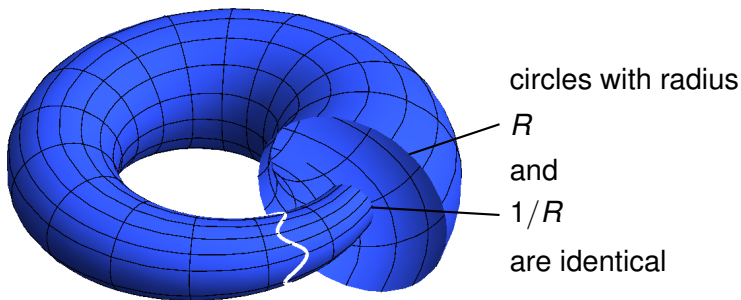
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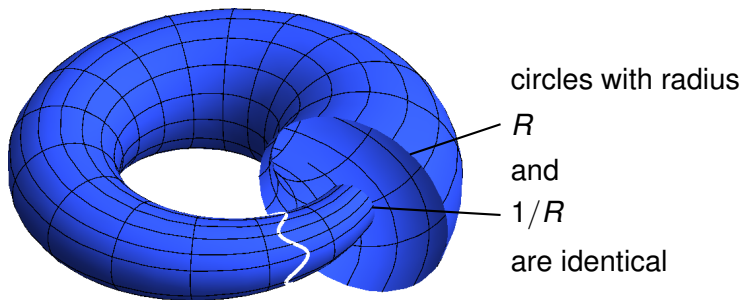
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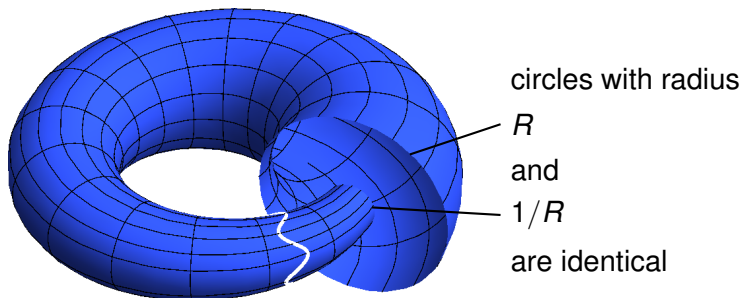
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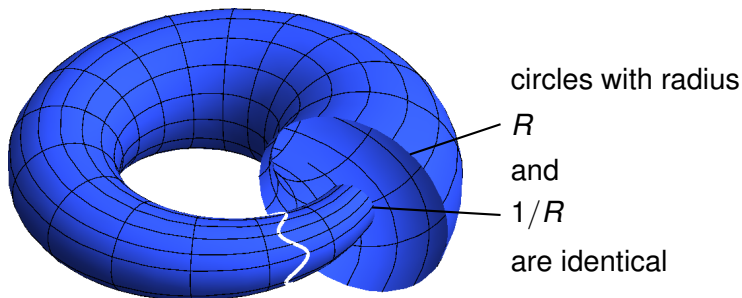
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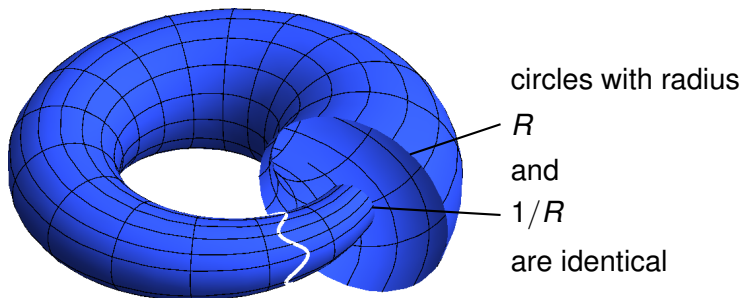
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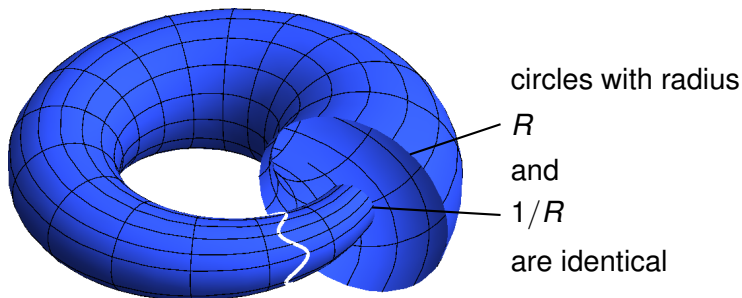
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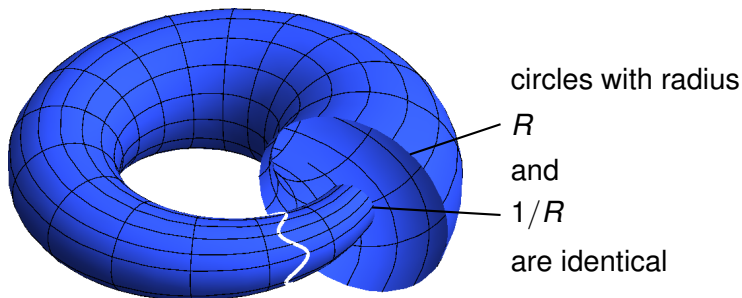


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~~SUGRA  
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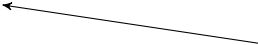
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 \mathcal{H}^{MN} &= \begin{pmatrix} g_{ij} - B_{ik} g^{kl} B_{lj} & -B_{ik} g^{kj} \\ g^{ik} B_{kj} & g^{ij} \end{pmatrix}
 \end{aligned}$$

## Gauge transformations and the strong constraint [7, 8]

- ▶ generalized Lie derivative

$$\mathcal{L}_\xi \mathcal{H}^{MN} = \xi^P \partial_P \mathcal{H}^{MN} + (\partial^M \xi_P - \partial_P \xi^M) \mathcal{H}^{PN} + (\partial^N \xi_P - \partial_P \xi^N) \mathcal{H}^{MP}$$
$$\mathcal{L}_\xi \phi' = \xi^M \partial_M \phi' + \frac{1}{2} \partial_M \xi^M$$

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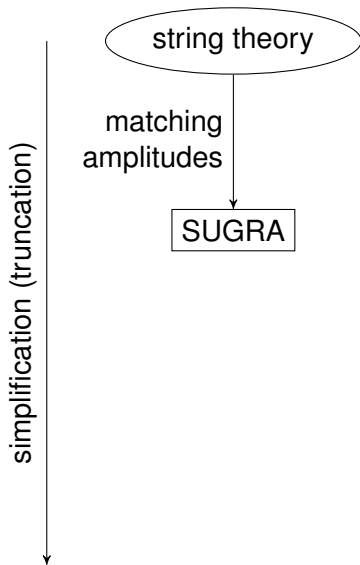
## Scherk-Schwarz compactification [9]

string theory

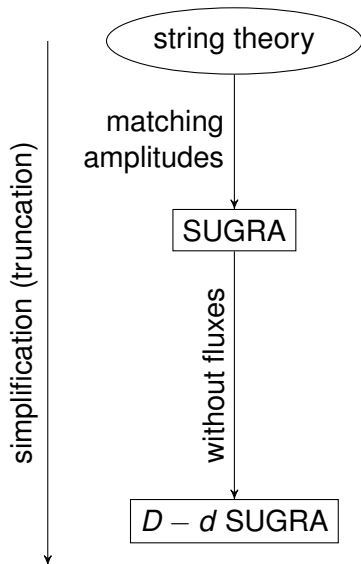
A diagram illustrating the Scherk-Schwarz compactification process. At the top, the text "string theory" is enclosed in a black oval. A vertical arrow points downwards from the oval, with the text "simplification (truncation)" written vertically along its left side.

simplification (truncation)

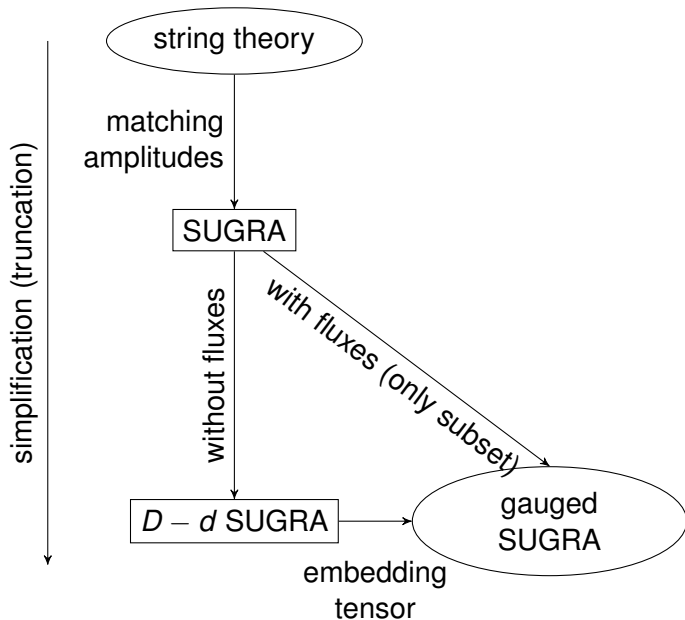
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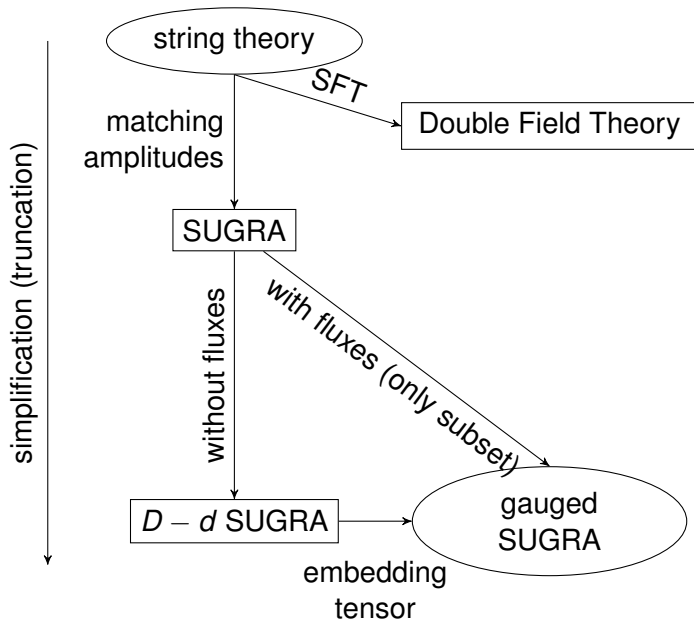
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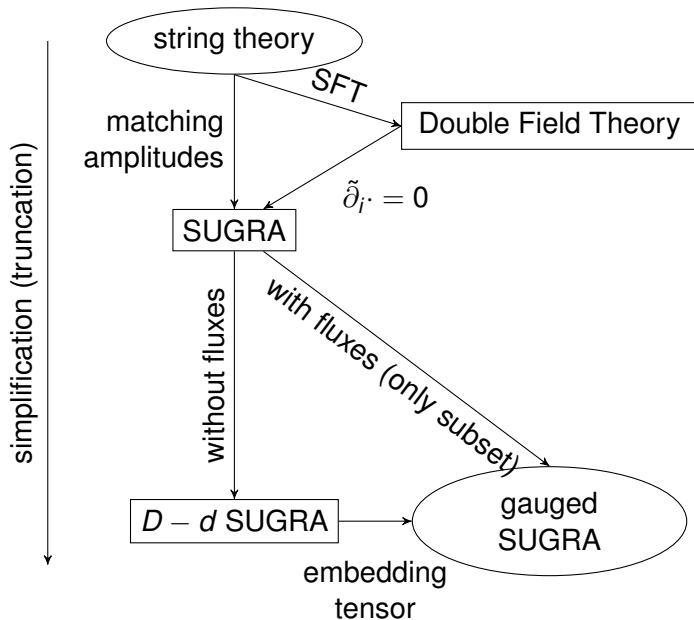
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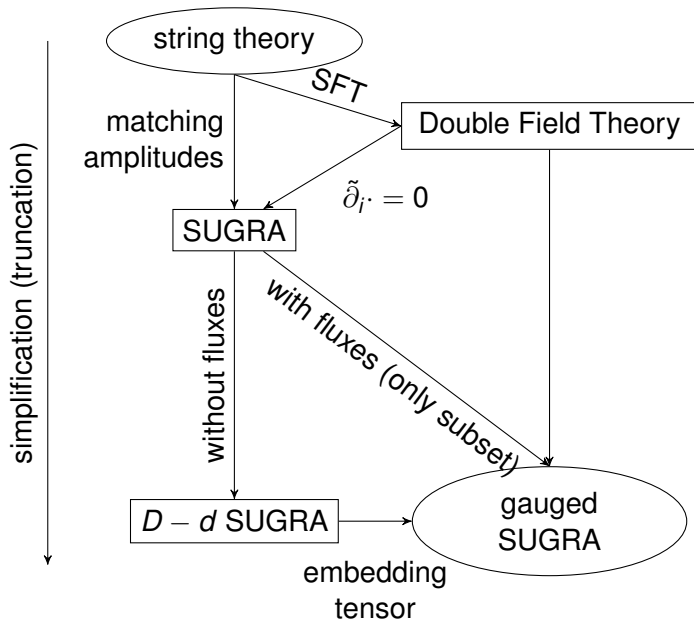
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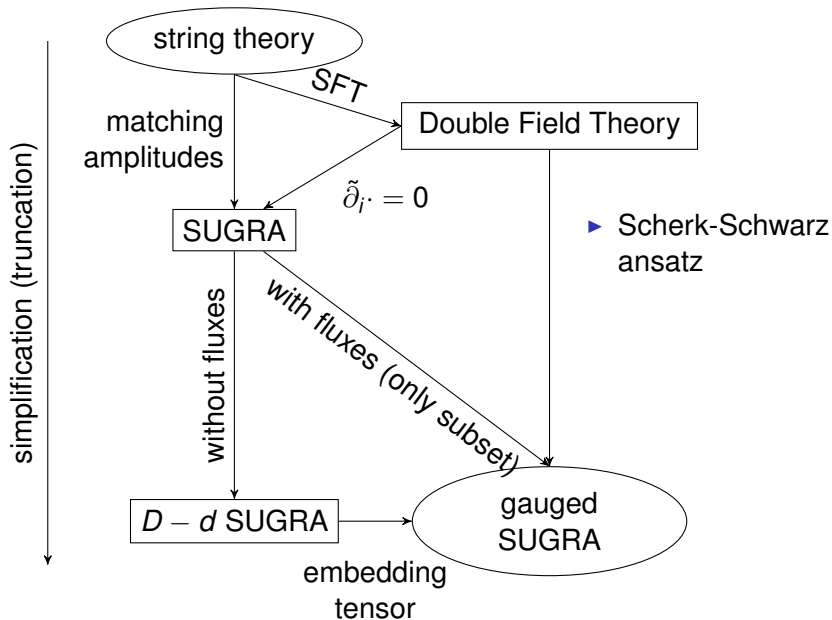
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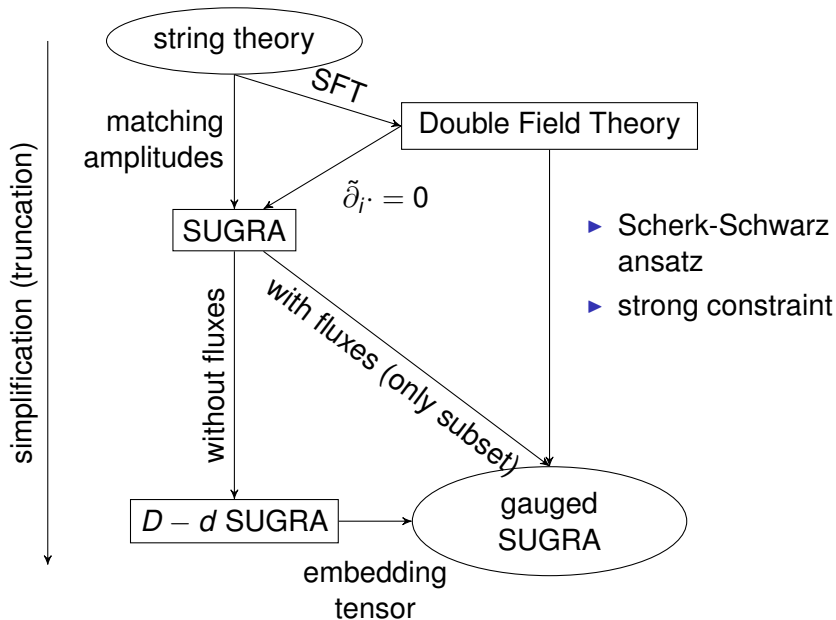


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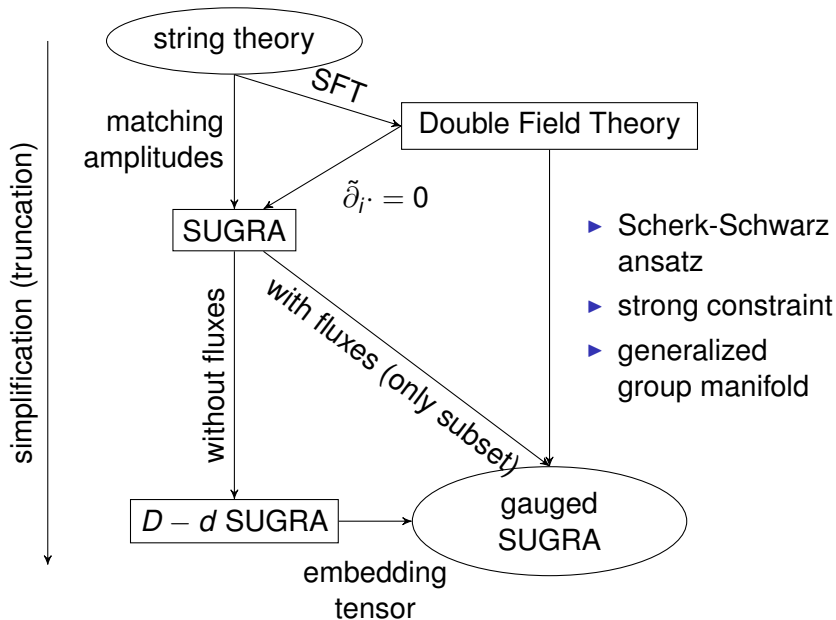




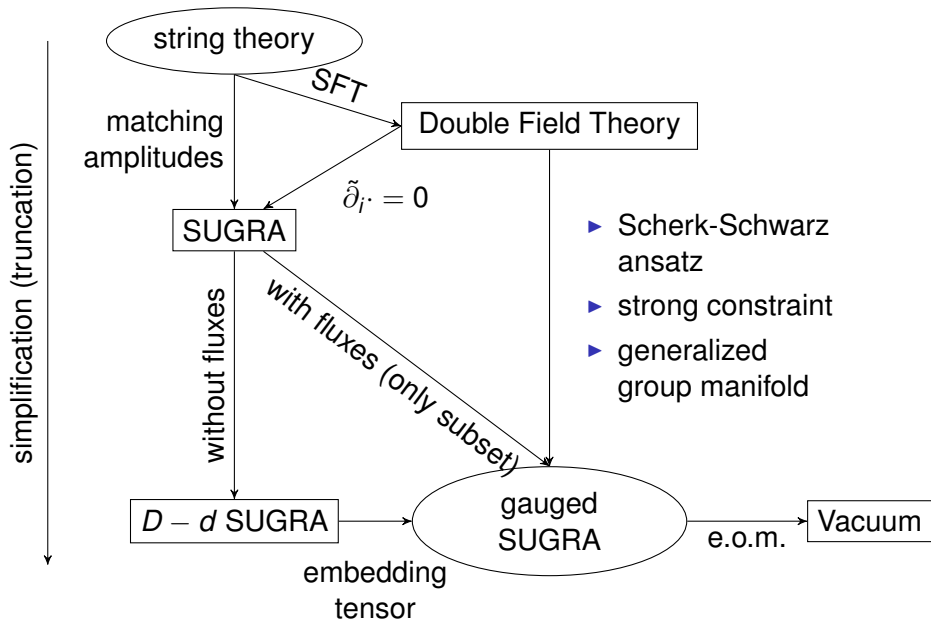
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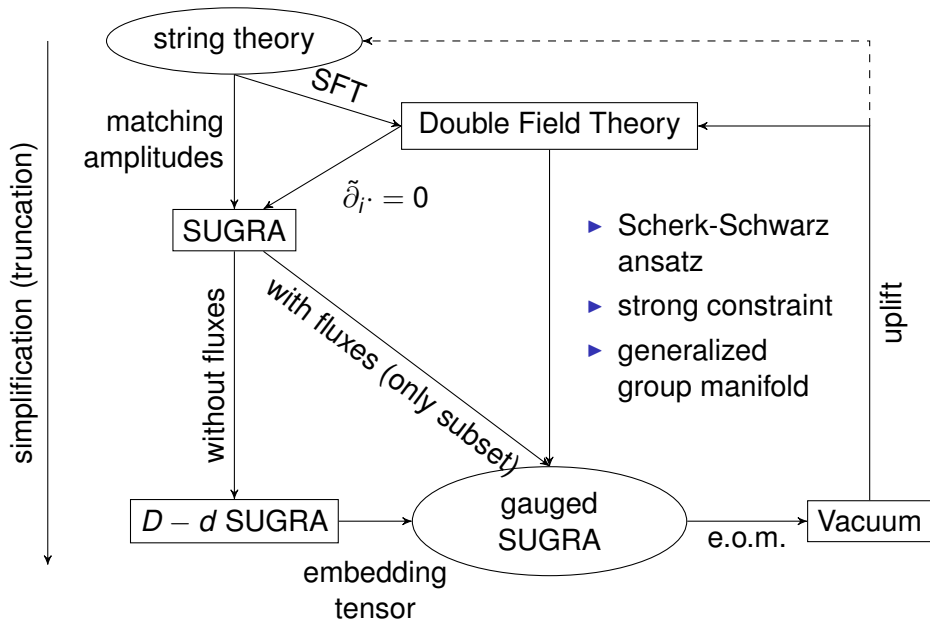
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# Scherk-Schwarz compactification [9] or a tool to construct backgrounds and fluctuations



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- ▶ DFT action + Scherk-Schwarz ansatz gives rise to

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- ▶ watch out for our publication on the arXiv 1312.????

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